

Administrators at a hospital believe that the number of beds in use is given by the function  $B(t) = 20\sin(t/10) + 50$ , where  $t$  is measured in days. For  $12 \leq t \leq 20$ , what is the minimum number of beds in use? (calc)

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**A.**

**30**

The velocity of a particle is given by  $v(t) = -2 + (t^2 + 3)^4$ . At  $t = 2.5$ , what direction is the particle moving? (calc)

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**B.**

**(0, 2)**

A car company introduces a new car for which the number of cars sold,  $S$ , is modeled by the function  $S(t) = 1500 - \frac{45}{t+2}$  where  $t$  is time in months.

Find the average rate of change of cars sold over the first 6 months. (calc)

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**C.**

**2**

If  $g(x) = 2x^2 - 4x$  on the interval  $[0, 5]$ , what is the absolute maximum of  $g(x)$ ? (no calc)

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**D.**

**-10.677**

For what value of  $c$  is the instantaneous rate of change for the function  $f(x) = 2\sqrt{x}$  equal to the average rate of change on the interval  $1 \leq x \leq 4$ ?

(no calc)

**E.**

**-3/10**

If  $f(x) = (x + 2)^{2/3}$  on  $[-5, 6]$ , what is the absolute maximum of  $f(x)$ ? (calc)

**F.**

**-8.941**

If  $c$  is the number that satisfies the conclusion of the Mean Value Theorem for  $f(x) = x^3 - 4x^2$  on  $[0, 2]$ , the  $c = ?$

(no calc)

**G.**

**221.937**

Find:

$$\lim_{x \rightarrow \infty} \frac{2x^2 + 3x}{x^3 + x + 1}$$

(no calc)

**H.**

**$\pi$**

If  $p(t) = e^{2t} - 6t$  represents the position function of a particle, when does the particle change directions? (calc)

I. **68.186**

If  $f(x)$  is continuous on  $[a, b]$ , what theorem can you use to find the absolute extrema of a function?  
(no calc)

J. **right**

$x$	0	2	3	4	6
$g(x)$	-3	1	5	2	1

$g(x)$  is a differentiable function on the interval  $[0, 6]$ . On what interval is there guaranteed to be a value of  $c$  such that  $g'(c) = 4$ ? (no calc)

K. **1/4**

$v(t) = (t + 1)(t + 3)^2$  is velocity of a particle where  $t$  is measured in minutes and  $v(t)$  is measured in inches per minute. Describe the speed of the particle at  $t = 2$  minutes. (calc)

L. **9.894**

$v(t) = (t - 1)(t - 3)^2$  is velocity of a particle where  $t$  is measured in minutes and  $v(t)$  is measured in inches per minute. At what interval is the particle moving to the right?

(no calc)

**M.**

**9/4**

If  $f(x)$  is continuous on  $[a, b]$  and differentiable on  $(a, b)$  and  $f(a) = f(b)$ , what theorem can you use to find the value of  $c$  on  $(a, b)$  such that  $f'(c) = 0$ ? (no calc)

**N.**

**0.549**

Find the point on the graph of  $f(x) = \sqrt{-x + 10}$  so that the point  $(2, 0)$  is closest to the graph.

(no calc)

**O.**

**increasing**

The area of a rectangle is 81 square feet. What dimensions of the rectangle would give the smallest perimeter? (no calc)

**P.**

**2.813**

Find:

$$\lim_{x \rightarrow 0} \frac{e^x - 1}{4x}$$

(no calc)

**Q.**

**9 by 9**

Find:

$$\lim_{x \rightarrow 1} \frac{x - 1}{\ln x - \sin(\pi x)}$$

(no calc)

**R.**

**Rolle's**

x	0	2	4	6	8	10	12	14	16
f(x)	1	5	8	10	11	10	8	5	1

Find the average rate of change of f(x) on the interval [4, 14].

(no calc)

**S.**

**0**

**T.**

**(1, 3) U (3, ∞)**

If  $f(x) = x^2 - 5x$  on the interval [0, 5], find the value of c such that  $f'(c) = 0$ .

(no calc)

A particle's position is given by  $p(t) = e^t \cos t$ , where  $p(t)$  is measured in centimeters and  $t$  is measured in seconds. What is the instantaneous acceleration at  $t = 1.5$ ?

(calc)

**U.** Mean Value

Apply the Mean Value Theorem to find the value(s) of  $c$  guaranteed for  $f(x) = x^3 - x^2 - 2x$  on  $[-1, 1]$ . (no calc)

**V.** 4

A particle moves along a line so that at time  $t$ , where  $0 \leq t \leq \pi$ , its position is given by  $s(t) = -4 \cos t - 2t$ .

What is the velocity of the particle when its acceleration is zero?

(no calc)

**W.** (2, 6)

If the velocity function is given by  $v(t) = \sin(\pi t)$ , what is the acceleration of this particle at  $t = 2$ ? (no calc)

**X.**  $\frac{1}{1 + \pi}$

Find the maximum volume of a box that can be made by cutting squares from the corners of an 12 inch by 18 inch rectangular sheet of cardboard and folding up the sides.

(calc)

**Y.** (2, 3)

A particle's position is given by  $p(t) = e^t \cos t$ , where  $p(t)$  is measured in centimeters and  $t$  is measured in seconds. What is the average velocity on  $[1, 3]$ ? (calc)

**Z.**  $2/3$

If  $f(x)$  is continuous on  $[a, b]$  and differentiable on  $(a, b)$ , then what theorem would you use to find  $f'(c) = \frac{f(a) - f(b)}{a - b}$ ? (no calc)

**AA.**  $(5/2, \sqrt{15/2})$

$x$	0	2	3	4	6
$g(x)$	-3	1	5	2	1

$g(x)$  is a differentiable function on the interval  $[0, 6]$ . On what interval is there guaranteed to be a value of  $c$  such that  $g(c) = -1$ ? (no calc)

**BB.**  $5/2$

If  $p(t) = e^{2t} - 8t$  represents the position function of a particle, what is the total distance the particle travels on  $[0.5, 1.5]$ ? (calc)

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**CC.** Extreme Value

$x$	0	2	3	4	6
$g(x)$	-3	1	5	2	1

$g(x)$  is a differentiable function on the interval  $[0, 6]$ . On what interval is there guaranteed to be a value of  $c$  such that  $g'(c) = 0$ ? (no calc)

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**DD.** -1/3