

Intermediate Value Theorem

In order for the theorem to be applicable...

- 1) $f(x)$ must be continuous on $[a, b]$
- 2) $f(c)$ must be between $f(a)$ and $f(b)$

Theorem states...

There exists at least one value, $x = c$, on (a, b) such that $f(c) = y$.

Extreme Value Theorem

In order for the theorem to be applicable...

- 1) $f(x)$ must be continuous on $[a, b]$

Theorem states...

There exists an absolute maximum and an absolute minimum on $[a, b]$ at either $x = a$, $x = b$, or any value of x on (a, b) such that $f'(x) = 0$ or $f'(x)$ is undefined.

Rolle's Theorem

In order for the theorem to be applicable...

- 1) $f(x)$ must be continuous on $[a, b]$
- 2) $f(x)$ must be differentiable on (a, b)
- 3) $f(a)$ must equal $f(b)$

Theorem states...

There exists at least one value, $x = c$, on (a, b) such that $f'(c) = 0$.

Mean Value Theorem

In order for the theorem to be applicable...

- 1) $f(x)$ must be continuous on $[a, b]$
- 2) $f(x)$ must be differentiable on (a, b)

Theorem states...

There exists a value, $x = c$, on (a, b) such that $f'(c) = \frac{f(a) - f(b)}{a - b}$.