Day 6 Notes: Polar Graphs & Arc Length

<u>ARC LENGTH:</u> Let *s* be the length of an arc of a curve. You must be able to find *s* for equations in rectangular, parametric, and polar forms.

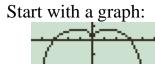
Rectangular:

$$s = \int_{a}^{b} \sqrt{1 + (f'(x))^{2}} dx$$
Parametric:

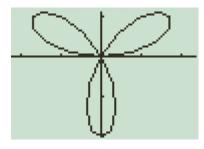
$$s = \int_{t_{1}}^{t_{2}} \sqrt{(x'(t))^{2} + (y'(t))^{2}} dt$$
Polar:

$$s = \int_{\theta_{1}}^{\theta_{2}} \sqrt{(r(\theta))^{2} + (r'(\theta))^{2}} d\theta$$

Example #1: Find the perimeter of the curve $r = 3(1 - \sin \theta)$.



Example #2: Find the perimeter of one petal of the rose curve $r = 2\sin(3\theta)$.



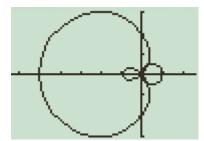
POINTS OF INTERSECTION OF POLAR GRAPHS

To find points of intersection, begin by graphing. Then solve the polar equations simultaneously. Sometimes, not all of the points of intersection will show up with the algebraic solution. Usually the missing points are at the pole.

- The points of intersection that you find algebraically are reached simultaneously (for the same values of Θ) in both graphs.
- The graphs may reach the pole at different values of Θ, which is why these solutions don't show up in the algebraic solution.

Note: When you are asked to find points of intersection, your answers will be in the form (r, Θ) .

Example #3: Find the points of intersection of the graphs of $r = 2 - 3\cos\theta$ and $r = \cos\theta$



Example #4: Find the points of intersection of the graphs of r = 2 and $r = 4\cos(2\theta)$.