Name: \_\_\_\_\_

AP Calculus BC Unit 11 – Day 4 – Warm-up

## AP<sup>®</sup> CALCULUS BC 2006 SCORING GUIDELINES (Form B)

## Question 2

An object moving along a curve in the xy-plane is at position (x(t), y(t)) at time t, where

$$\frac{dx}{dt} = \tan(e^{-t})$$
 and  $\frac{dy}{dt} = \sec(e^{-t})$ 

for  $t \ge 0$ . At time t = 1, the object is at position (2, -3).

(a) Write an equation for the line tangent to the curve at position (2, −3).

(b) Find the acceleration vector and the speed of the object at time t = 1.

(c) Find the total distance traveled by the object over the time interval  $1 \le t \le 2$ .

(d) Is there a time  $t \ge 0$  at which the object is on the y-axis? Explain why or why not.

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**#'s 1 & 2:** Plot the point in polar coordinates and find the corresponding rectangular coordinates for the point.

1) $(4, 3\pi/6)$	2) $(-4, -\pi/3)$

#'s 3 & 4: The rectangular coordinates of a point are given. Plot the point and find two sets of polar coordinates for the point for  $0 \le \theta \le 2\pi$ .

3) (1,1)	4) (-3, 4)

**#'s 5 – 8:** Convert the rectangular equation to polar form.

5) $x^2 + y^2 = a^2$	6) y = 4
7) $3x - y + 2 = 0$	8) $y^2 = 9x$

**#'s 9 – 12:** Convert the polar equation to rectangular form.

9) r = 3	10) $r = \sin\theta$
11) $\mathbf{r} = \mathbf{\theta}$	12) $r = 3sec\theta$

#'s 13 – 16: Name the type of polar curve. Graph the polar curve on your calculator and sketch the graph. Find an interval for  $\theta$  over which the graph is traced only once.

$13) r = 3 - 4\cos\theta$	$14) \mathbf{r} = 2 + \sin \theta$
$15) r = 2\cos(3\theta/2)$	16) $r^2 - 4\sin 2\theta$
13)1 - 2008(30/2)	10) 1 - 431120