

Find the Maclaurin series for
 $f(x) = \sin 2x$.

$$7 + \frac{(x-2)^2}{3^2 \cdot 2!} + \frac{3!(x-2)^4}{3^4 \cdot 4!}$$

Find the Taylor series for

$$f(x) = e^{-2x} \text{ about } x = 0.$$

$$2x - \frac{8x^3}{3!} + \frac{32x^5}{5!} - \dots$$

Given $f(x) = \sum_{n=0}^{\infty} \frac{(-1)^n x^{2n}}{(2n)!}$ find a power series for $f'(x)$.

$$1 - 2x + \frac{4x^2}{2!} - \frac{8x^3}{3!} + \frac{16x^4}{4!} - \dots$$

Write a power series, centered at 1, for the function $f(x) = \frac{3}{3-x}$ and then find the interval of convergence.

$$\sum_{n=1}^{\infty} \frac{(-1)^n x^{2n-1}}{(2n-1)!}$$

For what values of x does the

series $\sum_{n=0}^{\infty} \frac{2^n (x-4)^n}{n}$ converge?

$(-1, 3)$

Find the radius of convergence

for the power series $\sum_{n=0}^{\infty} \left(\frac{2x}{3}\right)^n$

$$\frac{7}{2} \leq x < \frac{9}{2}$$

Find the third-degree Taylor polynomial centered at 0 for the function $f(x) = e^{2x} + 3x$.

$$\frac{3}{2}$$

$$\text{If } f(x) = e^{-x^2} = 1 - x^2 + \frac{x^4}{2!} - \frac{x^6}{3!} + \dots$$

Write the first four nonzero terms of the

Taylor series for $\int_0^x e^{-t^2} dt$ about $x = 0$.

$$1 + 5x + 2x^2 + \frac{4}{3}x^3$$

Use the 4th degree Taylor Series for $\cos x$ about $x = 0$ to determine whether f has a relative minimum, relative maximum, or neither at $x = 0$.

$$x - \frac{1}{3}x^3 + \frac{1}{10}x^5 - \frac{1}{42}x^7$$

Let f be a function with derivatives of all orders and for which $f(2) = 7$. When n is odd, the n th derivative of f at $x = 2$ is 0. When n is even, and $n \geq 2$, the n th derivative of

f at $x = 2$ is given by $f^{(n)}(2) = \frac{(n-1)!}{3^n}$. Write a fourth degree Taylor polynomial for f about $x = 2$.

relative maximum