

AP Calculus AB
Unit 3 – Day 4 – Assignment

Name: *Answer Key*

In exercises 1 – 10, find the derivative of the function. Express your answer in simplest factored form.

1. $F(x) = x^3 e^{2x}$

$$F'(x) = (3x^2)(e^{2x}) + (x^3)(e^{2x})(2)$$

$$= 3x^2 e^{2x} + 2x^3 e^{2x}$$

$$= \boxed{x^2 e^{2x} (3 + 2x)}$$

2. $P(x) = e^{-2x^2}$

$$P'(x) = e^{-2x^2} (-4x)$$

$$= -4x e^{-2x^2}$$

$$= \boxed{\frac{-4x}{e^{2x^2}}}$$

3. $H(x) = e^{\ln x}$ product rule

$$H'(x) = e^{x \ln x} \left[(1)(\ln x) + (x)\left(\frac{1}{x}\right) \right]$$

$$= \boxed{e^{x \ln x} [\ln x + 1]}$$

4. $g(x) = (2x^2 + 3)e^x$

$$g'(x) = (4x)(e^x) + (2x^2 + 3)(e^x)(1)$$

$$= 4x e^x + 2x^2 e^x + 3e^x$$

$$= e^x (4x + 2x^2 + 3)$$

$$= \boxed{e^x (2x^2 + 4x + 3)}$$

5. $J(x) = \ln(e^{2x} + 1)$

$$J'(x) = \frac{e^{2x}(2)}{e^{2x} + 1}$$

$$= \boxed{\frac{2e^{2x}}{e^{2x} + 1}}$$

6. $F(x) = \ln(3 - 2x)$

$$F'(x) = \frac{-2}{3 - 2x}$$

$$= \frac{-2}{-(2x - 3)}$$

$$= \boxed{\frac{2}{2x - 3}}$$

$$\begin{aligned}
 7. \quad K(x) &= \ln \sqrt{5x-2} \\
 K(x) &= \ln(5x-2)^{1/2} \\
 K'(x) &= \frac{\frac{1}{2}(5x-2)^{-1/2}(5)}{(5x-2)^{1/2}} \\
 &= \frac{5}{2(5x-2)^{1/2}(5x-2)^{1/2}} \\
 &= \boxed{\frac{5}{2(5x-2)}}
 \end{aligned}$$

$$\begin{aligned}
 8. \quad F(x) &= x^2 e^{4x} \\
 F'(x) &= (2x)(e^{4x}) + (x^2)(e^{4x})(4) \\
 &= 2xe^{4x} + 4x^2 e^{4x} \\
 &= \boxed{2xe^{4x}(1+2x)}
 \end{aligned}$$

$$\begin{aligned}
 9. \quad T(x) &= \frac{\ln x}{x-2} \\
 T'(x) &= \frac{(x-2)\left(\frac{1}{x}\right) - (\ln x)(1)}{(x-2)^2} \\
 &= \frac{\frac{x-2}{x} - \ln x}{(x-2)^2} \quad (x) \\
 &= \boxed{\frac{x-2 - x \ln x}{x(x-2)^2}}
 \end{aligned}$$

$$\begin{aligned}
 10. \quad P(x) &= \frac{e^{2x}}{x^3} \\
 P'(x) &= \frac{(x^3)(e^{2x})(2) - (e^{2x})(3x^2)}{(x^3)^2} \\
 &= \frac{2x^3 e^{2x} - 3x^2 e^{2x}}{x^6} \\
 &= \frac{x^2 e^{2x}(2x-3)}{x^6} \\
 &= \boxed{\frac{e^{2x}(2x-3)}{x^4}}
 \end{aligned}$$

11. Find the equation of the tangent line to the graph of $y = \frac{\ln x}{4x}$ when $x = 1$.

$$\bullet \text{ P.O.T} \rightarrow f(1) = \frac{\ln(1)}{4(1)} = \frac{0}{4} = 0 \quad \boxed{(1, 0)}$$

$$\bullet \text{ S.O.T} \rightarrow f'(x) = \frac{(4x)\left(\frac{1}{x}\right) - (\ln x)(4)}{(4x)^2} = \frac{4-4\ln x}{16x^2}$$

$$f'(1) = \frac{4-4\ln(1)}{16(1)^2} = \frac{4-0}{16} = \boxed{\frac{1}{4}}$$

$$\boxed{y = \frac{1}{4}(x-1)}$$